KAKATIYA UNIVERSITY M.A/M.SC. MATHEMATICS Syllabus (w.e.f. 2019-20)

Semester - I
Paper – I
Paper Code: M1CP1
<u>ALGEBRA</u>

UNIT I

Isomorphism theorems on Groups - Normal Series - **Solvable** groups - Nilpotent groups (Chapter 5 : Sec 2 and Chapter 6 of Text Book 1)

UNIT II

Group Action on A set: The notation of a group action on a set - Isotropy subgroups - Orbits - Application of G-sets to counting.

Sylow Theorems: P-groups - Cauchy theorem - the Sylow theorems - Application of the Sylow theorems - Application to P-groups and the class equation - Further applications. (Sec 16,17,36,37 of Text Book 2)

UNIT III

The field of quotients of an integral domain: The construction - Uniqueness.

Rings of Polynomials: Polynomials in an indeterminate – A review – The evaluation homomorphism - Factorization of polynomials over a field - The Division algorithm in F[x] - Irreducible Polynomials - Eisenstein criterion - Uniqueness of factorization in F[x] - Prime fields - Application to unique factorization in F[x].

(Sec 21,22,23,27.17 to 27.27 of Text Book 2)

UNIT IV

Factorization: Unique factorization domains. Every PID is a UFD. If D is a UFD then D[x] is a UFD.

Euclidean Domains: Euclidean domains and Arithmetic in Euclidean domains.

Gaussian Integers and Multiplicative norms.

(Sect 45,46,47 of Text Book 2)

Text Book:

- 1.Basic Abstract Algebra by P.B. Bhattacharya, S.K.Jain, and S.R.Nagpaul, Second Edition, Cambridge University press.
- 2.A first Course in Abstract Algebra by John B.Fraleigh, Seventh Edition, Pearson education.

Reference Books:

- 1. Abstract Algebra by David S.Dummit, Richard M.Foote, Second edition, Wiley Student edition
- 2. Topics in Algebra by I.N Herstein
- 3. University algebra by N.Gopala Krishna.
- 4. Abstract Algebra by S.Lang.

M1CP2

M.A/M.SC. MATHEMATICS Syllabus (w.e.f 2019-20)

Semester - I Paper – II Paper Code: M1CP2 REAL ANALYSIS

UNIT I

Metric Spaces: Limit points – Closed sets – Open sets – Perfect Sets – Bounded Sets – Closure of a set - Compact sets – Connected sets.

Numerical sequences in metric spaces: Subsequences – Cauchy sequence – Dia-meter of a set – Definition of complete metric space.

Continuous functions in metric spaces: Characterization of continuity in terms of open sets and closed sets, Continuity and Compactness.

(Sec 2.15, 2.16, 2.18 - 2.38, 2.44 - 2.47, 3.1, 3.2, 3.5, 3.6(a), 3.7 - 3.11(a), (b), 3.12, 4.5 - 4.8, 4.13, 4.14, 4.18, 4.19, 4.22 of Text Book)

UNIT II

The Riemann-Stieltjes Integral: Definitions of partition – Refinement of partition and RS-Integral, Necessary and Sufficient condition for integrability, Integral as a limit of a sum. Integrability of continuous, Monotonic, discontinuous and composite functions.

Properties of the Integral: Integrability of sum and product of two functions – Integrability of modulus of a function – Integrators as step functions – Conversion of RS – Integral to Riemann integral.

(Sec 6.1 - 6.17, 6.19 of Text Book)

UNIT III

Sequences and Series of Functions: Pointwise and Uniform Convergence - Cauchy criterion for uniform convergence - Weirstrass M_n - test - Uniform convergence and Continuity - Uniform convergence and Integrability - Uniform convergence and differentiability - Equi continuous families of functions

(Sec 7.1 - 7.14, 7.16 - 7.25 of Text-book)

UNIT IV

Weirstrass approximation theorem – Definition of uniformly closed algebra – Stone's generalization of the Weirstrass theorem.

Power Series: Radius of Convergence – Real Power Series – Continuity and Differentiability of Power Series – Abel's theorem – inversion in the order of summation - Taylor's theorem – Identical power series.

(Sec 3.38 - 3.40, 7.26 - 7.32, 8.1 - 8.5 of Text-book)

Text Book:

Principles of Mathematical Analysis by Walter Rudin, McGraw – Hill, 3rd Edition

Reference books:

- 1. Mathematical Analysis by S.C.Malik and Savita Arora, S.Chand, 4th Edition
- 2. Mathematial Analysis by T.Apostle, Narosa.

M₁CP₃

KAKATIYA UNIVERSITY M.A/M.Sc. MATHEMATICS Syllabus(w.e.f.2019-20)

Semester – I Paper – III Paper Code: M1CP3

ORDINARY DIFFERENTIAL EQUATIONS

UNIT I

<u>Integration in series</u>: Ordinary and singular points – power series solution at ordinary point-Frobenius method – Problems on type I , type II , type III and type IV – series solution about regular singular point at infinity.

(Chapter 8: Sec 8.1 to 8.14 of Text Book 1)

UNIT II

<u>Linear equations with variable coefficients</u>: Introduction – Initial value problem for homogeneous equation – The Wronskian and linear dependence – reduction of the order of homogeneous equation – The non homogeneous equation. (Sec 3.1 to 3.6 of Text Book 2)

UNIT III

<u>Existence and uniqueness of solution of first order equation:</u> The method of successive approximation – The Liptsctitz condition – Sturm-Liouville problem – Orthogonality of eigen functions and Reality of eigen functions.

(Sec 5.4 to 5.5 of Text Book 2 and Sec 15.10 to 15.12 of Text Book 1)

UNIT IV

<u>Variational problems with fixed boundaries</u>: Euler's equation for functional containing first order derivative and one independent variable – Extremals – Functional dependent on higher order derivatives – Functions dependent on more than one independent variable – Variational problem in parametric form – Invariance of Euler's equation under coordinate transformation.

(Chapter 1 of part V of Text Book 1)

Text book

- 1. Advanced differential equations, M.D. Raisingania, S. Chand Company Ltd.
- 2. An introduction to ordinary differential equations by E.A. Coddington Prentice-Hall of India Pvt. Lted.

Referene books:

- 1. Differential equations with applications and Historical notes by George F. Simmons
- 2. Theory of ordinary differential equations by Somasundaram Narosa.

KAKATIYA UNIVERSITY M.A/M.Sc. MATHEMATICS Syllabus(w.e.f. 2019-20)

Semester - I
Paper – IV
Paper code: M1CP4
DISCRETE MATHEMATICS

UNIT I: Fundamentals of Logic

Fundamentals of logic-Logical inferences - Methods of proof of an implication – First order logic and other methods of proof - Rules of inference for propositions - Rules of inference for quantified propositions.

(Sec 1.5, 1.6, 1.7, 1.8 up to De Morgan Laws, 1.9 of Text Book)

UNIT II: Permutations and Combinations

Enumerating combinations and permutations with repetitions- Enumerating permutations with constrained repetitions- The principle of inclusion and exclusion.

(Sec 2.1 to 2.5, 2.8 of Text Book)

UNIT III: Recurrence Relations

Generating function of sequences – Calculating coefficients of generating functions-Recurrence relations- Solving recurrence relations by substitution and generating functionsthe method of characteristic roots – solutions of inhomogeneous recurrence relations.

(Sec 3.1 to 3.6 of Text Book)

UNIT IV: Boolean Algebra

Introduction, Boolean algebras – Boolean polynomials – Disjunctive and Conjunctive normal forms – Switching functions.-minimijation of switching functions.

(Sec 6.1 to 6.5 of Text Book)

Text Book:

Discrete Mathematics for Computer Scientists and Mathematicians by J.L.Mott, A. Kandel, and T.P. Baker

Reference Books:

- 1. Discrete Mathematical structures by Roden.
- 2. Discrete Mathematics by Kolman.
- 3. A Text book of Discrete Mathematics by Tremblay and Manohar.
- 4. Elements of Discrete Mathematics by C.L.Liu, McGraw Hill Company

KAKATIYA UNIVERSITY M.A/M.Sc. MATHEMATICS Syllabus(w.e.f.2019-20)

Semester - I
Paper – V

Paper Code: M1CP5 FUNDAMENTALS OF STATISTICS

UNIT I

Moments–Pearson's β and γ coefficients -Skewness and Kurtosis

Probability Definitions-Addition Theorem-Conditional probability - Multiplication Law of probability - Baye's Theorem - Random Variables - Probability mass function - Probability density function.

(Chapter 2, 3, 4.2, 5.1 to 5.5.5 of Text Book)

UNIT II

Mathematical Expectation – Expectation of a function of a random variable – Addition and Multiplication theorem of expectation - Expectation of linear Combination of random variables – Covariance – Variance of linear combination on of random variables – Moment generating function – Chebychev's inequality – Correlation –Karl Pearson's coefficient of Correlation-Linear regression. Angle between two regression lines.

(Chapter 6.1 to 6.6.1, 7.1, 7.1.2, 7.5,10.1 to 10.4.2, 11.1 to 11.2.3 of Text Book)

UNIT III

Discrete Distributions - Bernoulli distribution - Moments of Bernoulli distribution - Binomial distribution - Moments - Moment generating function of Binomial distribution - Additive property of Binomial distribution - Poisson distribution - Moments of Poisson distribution - Geometric distribution - Lack of memory property.

(Chapter 8.1 to 8.4.1, 8.4.4 to 8.4.7, 8.5, 8.5.2, 8.5.3, 8.5.5, 8.5.8, 8.7 to 8.7.3 of Text Book)

UNIT IV

Continuous Distributions -Normal Distribution - Characteristics of Normal Distribution and normal probability curve - Moments of Normal Distribution - Area property- Gamma Distribution - Moment generating function of Gamma Distribution - Exponential distribution- Moment generating function of Exponential distribution- Lack of memory property.

(Chapter 9.1, 9.2, 9.2.2 to 9.2.5, 9.2.7 to 9.2.11, 9.5, 9.5.1, 9.5.3, 9.8, 9.8.1 of Text Book)

Text Book:

Fundamentals of Mathematical Statistics by S.C. Gupta & V.K.Kapoor, 11th Edition